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Aspects of sensitivity analysis for the traveling salesman problem

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Document Version

Publisher's PDF, also known as Version of record

Publication date:

1997

[Link to publication in University of Groningen/UMCG research database](#)

Citation for published version (APA):

Poort, E. S. V. D. (1997). *Aspects of sensitivity analysis for the traveling salesman problem*. [Thesis fully internal (DIV), University of Groningen]. s.n.

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Aspects of Sensitivity Analysis for the Traveling Salesman Problem

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Published by: Labyrint Publication
P.O. Box 662
2900 AR Capelle a/d IJssel
The Netherlands
fax 31 (0)10-2847382

Printed by: Ridderprint, Ridderkerk

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ISBN 90-72591-45-3



Rijksuniversiteit Groningen

ASPECTS OF SENSITIVITY ANALYSIS FOR THE
TRAVELING SALESMAN PROBLEM

Proefschrift

ter verkrijging van het doctoraat in de
Economische Wetenschappen
aan de Rijksuniversiteit Groningen
op gezag van de
Rector Magnificus Dr. F. van der Woude
in het openbaar te verdedigen op
donderdag 6 november 1997
des namiddags te 4.15 uur

door

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geboren op 7 februari 1968
te Eindhoven

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Acknowledgments

It is a great pleasure for me to present the results of my Ph.D.-research carried out at the department of Econometrics of the University of Groningen. During the last five years, I wrote this dissertation under the supervision of Gerard Sierksma and Jack van der Veen. At this place, I like to take the opportunity to thank both of them for their supervision and support. I learned from them that doing good research takes patience and that one has to listen very carefully to the ideas and comments of other people.

As part of my research, I had the opportunity to work together with Marek Libura from Warszawa, Poland. It was a great pleasure and a privilege for me to spend a couple of months at the Systems Research Institute of the Polish Academy of Sciences in Warszawa in the spring of '94 and the spring of '95. In the spring of '95, Marek Libura also visited the department of Econometrics in Groningen. Our cooperation resulted in a number of papers. But far more important, I will always remember his hospitality and friendship.

In fact, there are two more people who have contributed to parts of this thesis. Firstly, a part of the research in Chapter 2 has been carried out together with Vladimir Dimitrijević of Belgrade, Yugoslavia, who visited the department in the summer of '93. Unfortunately, our cooperation did not continue due to the situation in Yugoslavia. Secondly, I like to mention Ruud Teunter. By his enthusiasm and good ideas, I was able to add Chapter 7 to my thesis.

At this place, I like to thank professor Casper Schweigman for his willingness to take the task as promotor as well as for his support and enthusiasm. Also the other members of my promotion committee, the professors Wim Hesselink, Jan Karel Lenstra, and Wim Klein Haneveld, are gratefully acknowledged for their interest in my work, their willingness to read the manuscript, and their useful suggestions for improvements.

As part of my position at the department of Econometrics, I supervised ten students writing their master thesis. Here I like to say that I appreciated the cooperation with all of them. I especially like to mention the master theses of Melvin de Jonge, Kees Jan Roodbergen, Sandor Steverink, and Reynold Zuil which have been of great use for my research. I also like to thank Joris Keizers who helped me programming one of the algorithms in Chapter 4.

I also want to mention professor René de Koster from the Erasmus University in Rotterdam. Our joint research on orderpicking problems resulted in two publications (not being included in this thesis), and there are possibly more to come.

A special thanks also goes to Erik Frambach for helping me with Latex, to Suwarni Bambang Oetomo for giving me secretarial support, to Evert Schoorl from the Graduate School/Research Institute Systems, Organizations, and Management (SOM) for his moral and financial support, and to my roommate Jan van der Ploeg who introduced me to the computer game FIFA.

Finally, I like to thank my family, especially my parents, my friends, and all people of the horseback riding club “Parafriid”. You have all been a great support to me. I would not have been able to write this thesis without you!

Edo van der Poort.

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